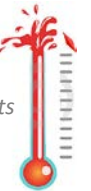


TRIG EQUATIONS & IDENTITIES QUIZ

34 %

Name: \_\_\_\_\_

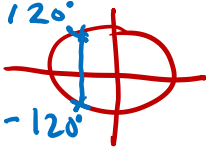
Fun-scale: off the charts



1. Consider the equation  $3\cos x - 5 = 5\cos x - 4$ .  
 (a) Algebraically determine any solutions on  $-180^\circ \leq x < 180^\circ$

2  $-2\cos x = 1$

$\cos x = -\frac{1}{2}$



$x = \pm 120^\circ$

- (b) State a general solution

1

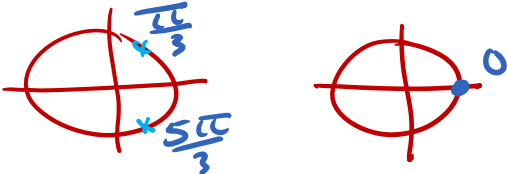
$x = 120^\circ + 360n$   
 $240^\circ + 360n$   
 $n \in \mathbb{I}$

2. Algebraically solve on  $0 \leq \theta < 2\pi$ .

2  $\rightarrow 2\cos^2 \theta - 3\cos \theta + 1 = 0$

$(2\cos \theta - 1)(\cos \theta - 1) = 0$

$\cos \theta = \frac{1}{2}$      $\cos \theta = 1$



$\theta = 0, \frac{\pi}{3}, \frac{5\pi}{3}$

3. Solve on  $0 \leq \theta < 360^\circ \rightarrow 3\csc \theta + 4 = 0$

2 Round answers to the nearest degree.

$\csc \theta = -\frac{4}{3}$

$\sin \theta = -\frac{3}{4}$

$\alpha = \sin^{-1}(3/4) \approx 49^\circ$   
 sin is Neg in III & IV

$\theta \approx 229^\circ$  or  $311^\circ$   
 (180 + 49)      (360 - 49)

4. Simplify each expression to one of the three primary trig functions. ( $\sin x$ ,  $\cos x$ , or  $\tan x$ )

a)  $\sec x \cot x \sin^2 x$

1  $\frac{1}{\cancel{\cos x}} \cdot \frac{\cancel{\cos x}}{\cancel{\sin x}} \cdot \frac{\cancel{\sin x} \sin x}{1}$

$= \sin x$

b)  $\frac{\sin x}{\tan x}$

$= \frac{\sin x}{\frac{\sin x}{\cos x}}$  Flip/ Mult.

$= \frac{\cancel{\sin x} \cdot \cos x}{\cancel{\sin x}}$

$= \cos x$

c)  $\frac{\sin 2\theta}{2\cos \theta}$

1  $\frac{2\sin \theta \cos \theta}{2\cos \theta}$

$= \sin \theta$

d)  $\frac{\cos 2\theta + 1}{2\cos \theta}$

$= \frac{\cos 2\theta}{2\cos \theta} + \frac{1}{2\cos \theta}$   
 $= \frac{2\cos^2 \theta - 1 + 1}{2\cos \theta}$

$= \frac{2\cos \theta \cancel{\cos \theta}}{2\cancel{\cos \theta}}$

$= \cos \theta$

e)  $\frac{\cos^3 x}{\cos 2x + \sin^2 x}$

$= \frac{\cos^3 x}{\cos^2 x - \cancel{\sin^2 x} + \cancel{\sin^2 x}}$   
 "cos 2x"

$= \frac{\cancel{\cos x} \cdot \cancel{\cos x} \cdot \cos x}{\cancel{\cos x} \cdot \cancel{\cos x}}$

$= \cos x$

5. Write each as a single trigonometric function.

a)  $\cos 43^\circ \cos 28^\circ - \sin 43^\circ \sin 28^\circ$

$= \cos(43^\circ + 28^\circ)$

$= \cos 71^\circ$

b)  $2\cos^2 \frac{\pi}{12} - 1$

$= \cos(2 \cdot \frac{\pi}{12})$

$= \cos \frac{\pi}{6}$

c)  $\frac{2\tan 76^\circ}{1 - \tan^2 76^\circ}$

$= \tan(152^\circ)$

Pattern is "cos(a+b)"      Pattern is "cos 2a"

3

4

7

3

6. Consider the equation  $\frac{\sec x}{\tan x + \cot x} = \sin x$
- a) Numerically verify the possibility of an identity using  $x = 60^\circ$ . What value do you get for both sides?

1

$$\frac{\frac{1}{\cos 60^\circ}}{\tan 60^\circ + \frac{1}{\tan 60^\circ}} = \frac{\frac{\sqrt{3}}{2}}{\frac{\sqrt{3}}{2} + \frac{2}{\sqrt{3}}} = \frac{\sqrt{3}}{2} \quad \sin 60^\circ = \frac{\sqrt{3}}{2}$$

- b) State the non-permissible values of the equation on the domain  $0^\circ \leq x < 360^\circ$

$\tan x \neq 0$     $\cot x \neq 0$   
 $x \neq 0, 180^\circ$     $x \neq 90, 270^\circ$

(c) BONUS Prove this identity (on scrap paper)

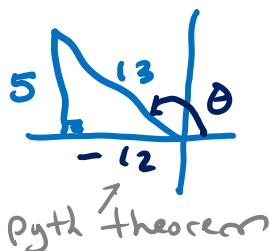
7. Simplify  $\cos(\frac{\pi}{2} - x)$  using a difference identity.

2

$$= \cos \frac{\pi}{2} \cos x + \sin \frac{\pi}{2} \sin x$$

$$= (0) \cos x + (1) \sin x \rightarrow = \sin x$$

8. Given that  $\theta$  is in quadrant II and  $\sin \theta = \frac{5}{13}$ , determine the exact value of:



a)  $\cos 2\theta$

$$\frac{2}{2} = 1 - 2\sin^2 \theta$$

$$= 1 - 2\left(\frac{5}{13}\right)^2$$

$$= \frac{119}{169}$$

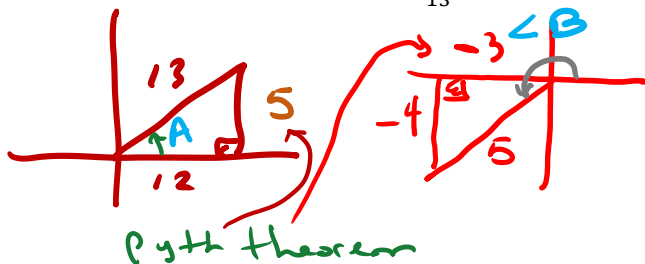
- b)  $\sin(\theta + 90^\circ)$

$$= \sin^2 \theta \cos 90^\circ + \cos \theta \sin 90^\circ$$

$$= \left(\frac{5}{13}\right)(0) + \left(-\frac{12}{13}\right)(1)$$

$$= -\frac{12}{13}$$

9. If  $\angle A$  is in quadrant I with  $\cos A = \frac{12}{13}$  and  $\angle B$  is in quadrant III with  $\sin B = \frac{4}{5}$ , evaluate  $\sin(A + B)$



$$= \sin A \cos B + \cos A \sin B$$

$$= \left(\frac{5}{13}\right)\left(-\frac{3}{5}\right) + \left(\frac{12}{13}\right)\left(-\frac{4}{5}\right)$$

$$= -\frac{63}{65}$$

10. Use an appropriate sum/difference formula to determine the exact value of: show all steps on scrap paper - provide simplified exact-value answers here

4

a)  $\sin 165^\circ = \frac{\sqrt{6} - \sqrt{2}}{4}$

b)  $\tan \frac{17\pi}{12} = \sqrt{3} + 2$   
 \* Show work!

11. Prove each identity

a)  $\frac{\cos x}{\cot x} * \csc x = 1$

| LS  | RS |
|---|----|
| $\frac{\cos x}{\cot x} * \csc x$                            | 1  |
| $= \frac{\cos x}{\frac{\cos x}{\sin x}} * \frac{1}{\sin x}$ |    |
| $= \cos x * \frac{\sin x}{\cos x} * \frac{1}{\sin x}$       |    |
| $= 1$   |    |

LS = RS

b)  $\sin x + \cos x \cot x = \csc x$

| LS   | RS                 |
|--|--------------------|
| $\sin x + \cos x \cot x$   | $\frac{1}{\sin x}$ |
| $= \frac{\sin x}{1} + \frac{\cos x \cdot \frac{\cos x}{\sin x}}{\sin x}$ |                    |
| $= \frac{\sin^2 x}{\sin x} + \frac{\cos^2 x}{\sin x}$                    |                    |
| $= \frac{\sin^2 x + \cos^2 x}{\sin x}$                                   |                    |
| $= \frac{1}{\sin x}$   |                    |

LS = RS !!